## EQF-Note 2016-10-02

Background for these notes is: Chris van Tienhoven: Encyclopedia of Quadri-Figures <u>http://www.chrisvantienhoven.nl/</u>

## **Dual Conics in the QA/QL-constellation**

In addition to EQF-Note 2016-09-22 here are described 2 x 4 dual conics in the QA/QL-constellation, using point and line isoconjugations:

- (1) Conics inscribed the diagonal triangle DT and circumscribed a QL-triangle.
- (2) Conics circumscribed the diagonal triangle DT and inscribed a QA-triangle.



Starting with a quadrangle QA and its diagonal triangle DT, the DT-trilinear polars of the QA-vertices give the dual QL with the same diagonal triangle.

- The *DT*-trilinear polars of points on a *QL*-line envelope a conic of type (1).
- The line isoconjugation *QL-Tf2* for the line pencil of a *QA*-vertex gives a conic of type (1).
- The isoconjugate of a *QL*-line wrt an isoconjugation for the remaining *QL*-trilateral with fixed point in the corresponding *QA*-vertex is a conic of type (1).

The dual interpretation:

• The *DT*-trilinear poles of lines through a *QA*-vertex give a conic of type (2).

- The isoconjugation *QA-Tf2* for a *QL*-line gives a conic of type (2).
- The line isoconjugate of the line pencil of a QA-vertex wrt a line isoconjugation for the remaining QA-triangle with fixed line in the corresponding QL-line gives a conic of type (2).

## Conclusion:

• The conics of type (1) are the duals of the conics of type (2).

Additional remarks:

- The centers of the four conics of type (1) lie on a *DT*circumscribed conic through *QL-P8*, *QL-P13*, *QL-P24*.
- The centers of the four conics of type (1) are the duals of parallels to the *QL*-lines two thirds distance to the corresponding *QA*-vertex.
- The centers of the four conics of type (2) are the duals of parallels to the *QL*-lines one third distance to the corresponding *QA*-vertex.

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